

# Limits of geostrophic dynamics at the ocean surface: Guidance for planning SWOT's mission and products

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**geostrophic analysis:** measure  $\eta$  and calculate  $\mathbf{u} \approx \mathbf{u}_g$  from

$$\mathbf{u}_g = \frac{g}{f} \hat{\mathbf{z}} \times \nabla_h \eta$$

with the presumption that it is superimposable with wind-driven Ekman currents.

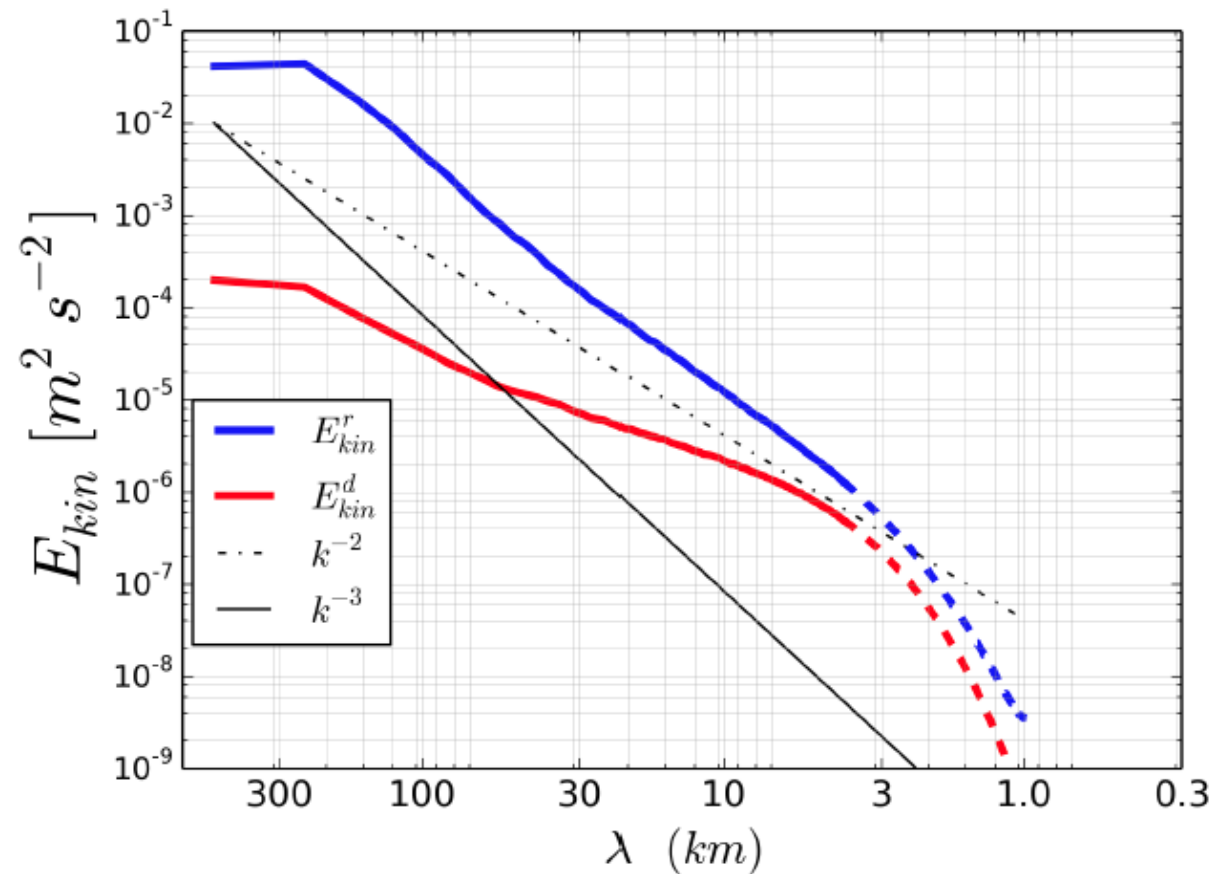
This framework has served us very well for present altimetry measurements of **large-mesoscale** eddies with wavelength  $\lambda > 100\text{-}200$  km.

At smaller  $\lambda$  this relation begins to be **inaccurate**. Consider a Helmholtz decomposition of surface velocity:  $\mathbf{u}_h = \mathbf{u}_{rot} + \mathbf{u}_{div}$  .

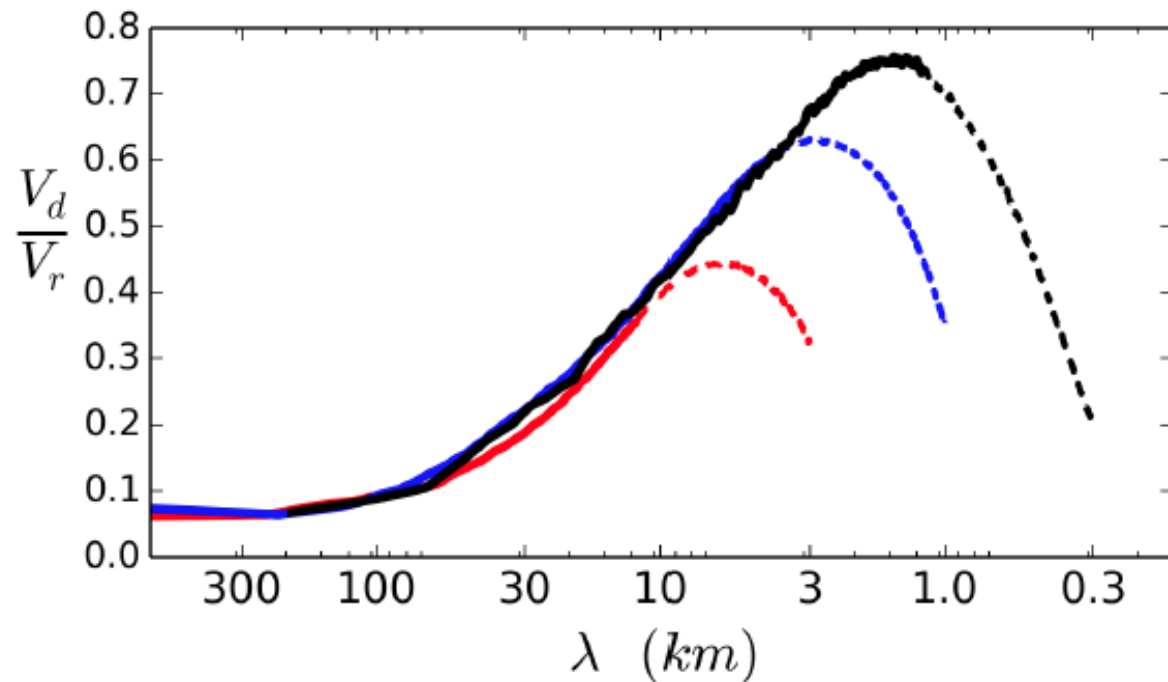
- The cyclostrophic correction to geostrophic balance often matters.
- $\mathbf{u}_{div}$  becomes comparable to  $\mathbf{u}_{rot}$  .
- $\eta$  has internal wave components that contaminate  $\mathbf{u}_g$  , even though  $\mathbf{u}_h$  itself is mostly balanced.

e.g., the Gulf Stream with several nested resolutions

kinetic energy  
spectrum  
components  
( $\Delta x = 500$  m)



divergent/rotational ratio  
( $\Delta x = 1.5, 0.5, 0.15$  km)



“geostrophic”/rotational ratio  
( $\Delta x = 1.5, 0.5, 0.15$  km)

